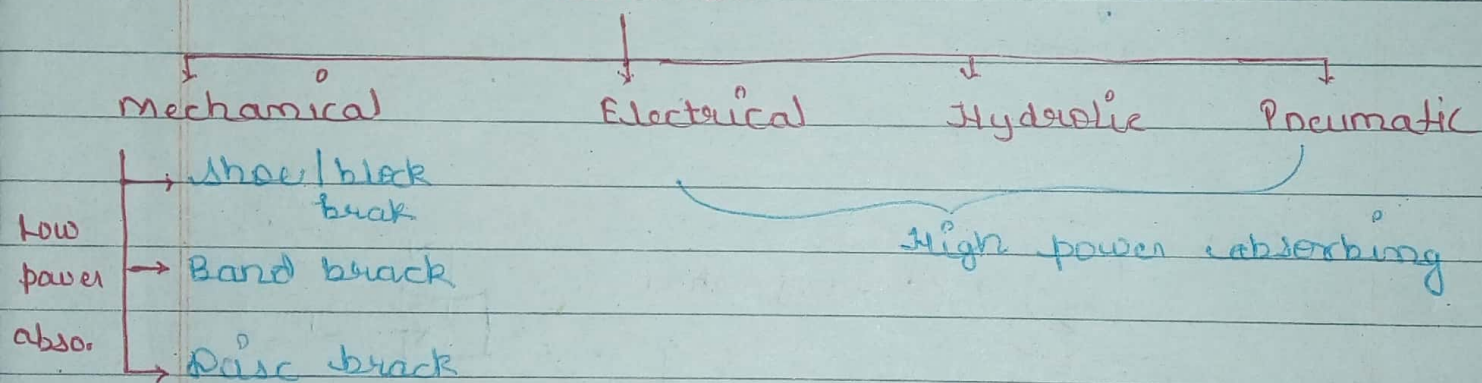


## • Brakes

Brakes are devices that dissipate kinetic energy of moving part of machine.

In (ME) brake the deceleration is achieved through sliding friction b/w a stationary object & a rotating part.

## • Brakes



→ Shoe brake  
force applied  
radially

→ Band brake  
force applied  
tangentially

→ Disc brake  
force applied  
axially

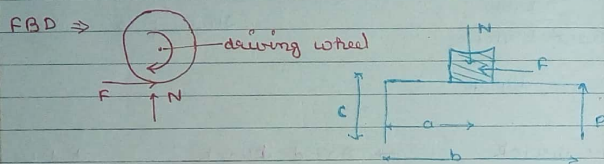
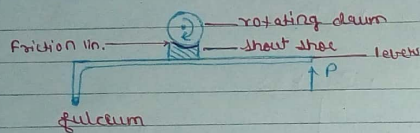
## • Band brake

→ Simple band brake

→ Differential band brake.

### \* shoe / Block / Drum brake

- In a shoe brake the rotating drum is brought in contact with the shoe by suitable force.
- The contacting surface of the shoe is coated with friction material.



$$\Rightarrow \sum M = 0$$

$$\Rightarrow Pb + FC = Na$$

$$\Rightarrow Pb = Na - FC$$

$$\Rightarrow P = \frac{Na - FC}{b}$$

$$\Rightarrow P = \frac{N(a - \mu c)}{b}$$

$$[F = \mu N]$$

P → actuating force  
Applied force  
Braking force

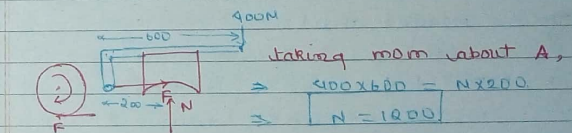
case I  $P = +ve \rightarrow a > \mu c \rightarrow$  desirable condition

\*\* when the moment due to applied force (Pb) & moment due to friction force (FC), both are acting in same direction that means friction force help to reduce the value of braking force this type of brake are known as self-energizing brakes

case II :  $P = 0 \rightarrow a = \mu c$  self locking

case III :  $P = -ve \rightarrow a < \mu c$  out of control

Q. A block brake shown below has a face width of 300 mm & a mean coefficient of friction of 0.25 for an actuating force of 400 N the braking torque.



$$\rightarrow F = \mu N$$

$$\rightarrow F = 1200 \times 0.25$$

$$\rightarrow F = 300 \text{ N}$$

$$\rightarrow BT = F \times r$$

$$\rightarrow BT = 300 \times 150 \times 10^{-3}$$

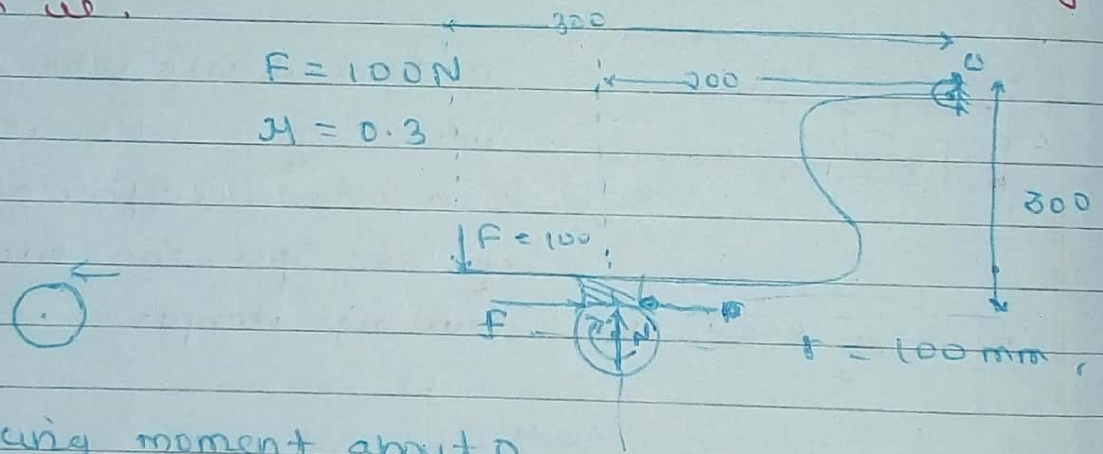
$$\rightarrow BT = 45 \text{ N-m}$$



• Steps to solving numerical  $\Rightarrow$

- observe the sense of rotation of drum.
- acc. to sense draw FBD.
- calculating moment about the fulcrum.

Q A schematic of an external drum rotating clockwise engaging with a short shoe as shown fig. The shoe is mounted at  $X$  on a rigid lever pivoted at point  $O$ . A force  $F = 100\text{ N}$  is applied at the free end of the lever given that  $\mu = 0.3$ , the BT in Nm applied by drum is.



Taking moment about O

$$\Rightarrow F \times 300 + f \times 300 = N \times 200$$

$$\Rightarrow 100 \times 300 + 0.3 \times N \times 300 = N \times 200$$

$$\Rightarrow 30000 + 90N = 200N$$

$$\Rightarrow (200 - 90)N = 30000$$

$$\Rightarrow N = 272.72$$

$$\Rightarrow f = \mu N$$

$$\Rightarrow f = 0.3 \times 272.72$$

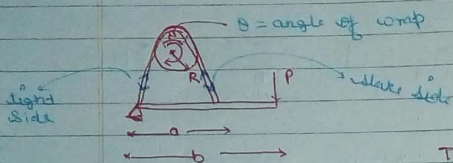
$$\Rightarrow f = 81.81$$

$$\rightarrow BT = 81.81 \times 100 \times 10^{-3}$$

$$BT = 8.18 \text{ N-m}$$

### \* Simple band brake

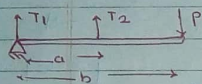
When one end of the band passes underneath the fulcrum of lever then it's known as simple band brake.



$$\frac{T_1}{T_2} = e^{\mu \theta}$$

$T_1$  = tension on tight side  
 $T_2$  = tension on slack side  
 $\mu$  = coefficient of friction  
 $\theta$  = angle of wrap  
 $e^{\mu \theta} \rightarrow$  radian

FBD

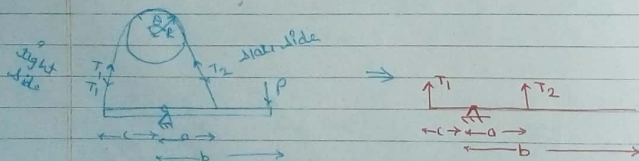


$$Pb + T_1 \times 0 = T_2 b$$

$$\Rightarrow P = \frac{T_2 a}{b}$$

\* Braking torque  $\Rightarrow T_F = (T_1 - T_2) R$  (radius of drum)

### \*\* Differential band brake



$$\Rightarrow \mu \theta = 0$$

$$\Rightarrow T_1 c + P b = T_2 a$$

$$\Rightarrow P = \frac{T_2 a - T_1 c}{b}$$

$$\Rightarrow P = \frac{T_2}{b} \left[ a - \frac{T_1}{T_2} c \right]$$

$$\Rightarrow P = \frac{T_2}{b} \left[ a - e^{\mu \theta} c \right] \rightarrow \frac{T_1}{T_2} = e^{\mu \theta}$$

$$\rightarrow T_F = (T_1 - T_2) R$$

\* For self locking  $\left[ a = e^{\mu \theta} c \right]$   
 $P \rightarrow 0$

When neither of the band brake passes to the fulcrum of lever then it is known as differential band brake.

Q In a band brake the ratio of tight side band tension to the tension on slack side is 3, if the angle of overlap of band on drum is  $180^\circ$ , the coefficient of friction between band & drum is

$$\Rightarrow \frac{T_1}{T_2} = e^{\mu \theta}$$

$$\Rightarrow 3 = e^{180^\circ \times \mu}$$

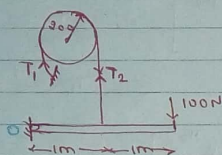
$$\Rightarrow \ln 3 = 180^\circ \times \mu$$

$$\Rightarrow \ln 3 = 180^\circ \times \frac{\pi}{180} \times \mu$$

$$\Rightarrow \mu = \frac{\ln 3}{\pi} = 0.949 \approx 0.35$$



Q A band brake consists of a lever attached to one end of the band. The other end of the band is fixed to ground. The wheel has a radius of 200 mm & a wrap angle of band is  $3\pi$ . The braking force applied to drum is limited to 100 N, &  $\mu = 0.5$ .



$$\frac{T_1}{T_2} = e^{\mu \theta}$$

$$\frac{T_1}{T_2} = 10.550$$

$$T_2 = 200$$

- The max tension that can be generated during braking is?
- The max wheel torque that can be completely brake is.

SM = 0 about O

$$T_2 \times 1 = 100 \times 2$$

$$T_2 = 200 \text{ N}$$

$$T_1 = 200 \times 10.550$$

$$T_1 = 2110 \text{ N}$$

$$BT = (2110 - 200) \times 200$$

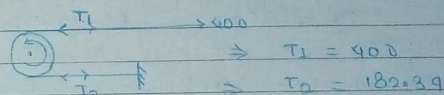
$$BT = 382 \text{ N-m}$$

Q Force of 400 N is applied to the brake drum of 0.5 m diameter in a band brake like as shown in fig when  $\theta = 180^\circ$ , if  $\mu = 0.25$  the BT applied in N-m is,

$$\frac{T_1}{T_2} = e^{\frac{180 \times \pi}{180} \times 0.25}$$

$$\frac{T_1}{T_2} = 8.193$$

$$T_1 = 8.193 T_2$$



$$BT = (T_1 - T_2) r$$

$$BT = (400 - 182.39) \times 0.25$$

$$BT = 54.40 \text{ N-m}$$

Q The forces  $F_1$  &  $F_2$  in a brake band & the radius of drum are shown in fig. The  $\mu$  is 0.25.  $\Delta \theta = \frac{3\pi}{2}$  radian. It is given that  $r = 1 \text{ m}$  &  $F_2 = 1 \text{ N}$ . The torque in N-m is?

$$\frac{T_1}{T_2} = e^{\mu \theta}$$

$$\frac{T_1}{T_2} = e^{\frac{3\pi}{2} \times 0.25}$$

$$\frac{T_1}{T_2} = 3.24818$$

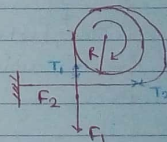
$$T_1 = F_1 \quad T_2 = 1 \text{ N}$$

$$T_2 = F_2 \quad T_1 = 3.24818$$

$$BT = (T_1 - T_2) r$$

$$BT = (3.24818 - 1) \times 1$$

$$BT = 2.24818$$

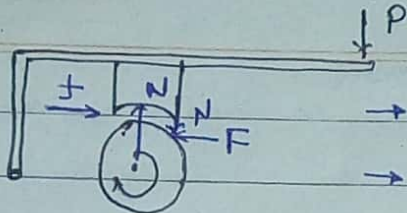


• Short - NOTE

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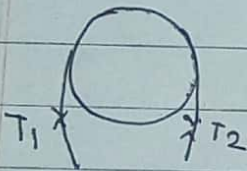
$$\rightarrow F = \mu N$$

$$\rightarrow P = +ve \text{ (desirable)} \quad a > \mu c$$

$$\rightarrow P = 0 \text{ (self locking)} \quad a = \mu c$$

$$\rightarrow P = -ve \text{ (out of control)} \quad a < \mu c$$

\*



$$\frac{T_1}{T_2} = e^{\mu \theta}$$

$$BT = (T_1 - T_2) R$$

BT  $\rightarrow$  braking torque